

## Abstract

Studies of double beta ( $2\nu\beta\beta$ ) decay to various excited states in different isotopes provide valuable insights into nuclear structure models. The AMoRE, which utilizes an array of  $^{100}\text{Mo}$ -enriched  $\text{CaMoO}_4$  and  $\text{Li}_2\text{MoO}_4$  crystal scintillators, is advantageous for investigating  $2\nu\beta\beta$  decay of  $^{100}\text{Mo}$  to the excited states of  $^{100}\text{Ru}$ .

In the AMoRE-I phase, we measured the half-life of  $2\nu\beta\beta$  transition of  $^{100}\text{Mo}$  to the  $0_1^+$  state of  $^{100}\text{Ru}$  using a total of 16 crystal detectors, and the half-life value is  $(6.83 \pm 0.71 \text{ (stat)} \pm 0.32 \text{ (sys)}) \times 10^{20}$  years. The half-life limit for the  $2\nu\beta\beta$  transition to the  $2_1^+$  state of  $^{100}\text{Ru}$  is set as  $2.5 \times 10^{21}$  years (90% C.I.).

A prospective study of  $2\nu\beta\beta$  decay to the excited states of  $^{100}\text{Ru}$  has been conducted for AMoRE-II. Considering the increased crystal mass and measurement time, the error-to-signal ratio for the  $2\nu\beta\beta$  decay of  $^{100}\text{Mo}$  to the  $0_1^+$  state is expected to decrease significantly from 6.3% to 0.3%. The half-life sensitivity to the  $2\nu\beta\beta$  decay of  $^{100}\text{Mo}$  to  $2_1^+$  state of  $^{100}\text{Ru}$  in AMoRE-II is estimated as limit  $T_{1/2} \sim 1.20 \times 10^{23}$  years. The triple-crystal-hit conditions event can be measured in AMoRE-II, that will be useful for observing the pure elections energy distribution.

## Study motivation: $2\nu\beta\beta$ decay to excited states of $^{100}\text{Mo}$

### Half life and NME of $2\nu\beta\beta$ decay

$$(T_{1/2}^{2\nu})^{-1} = G_{2\nu} |M^{2\nu}|^2$$

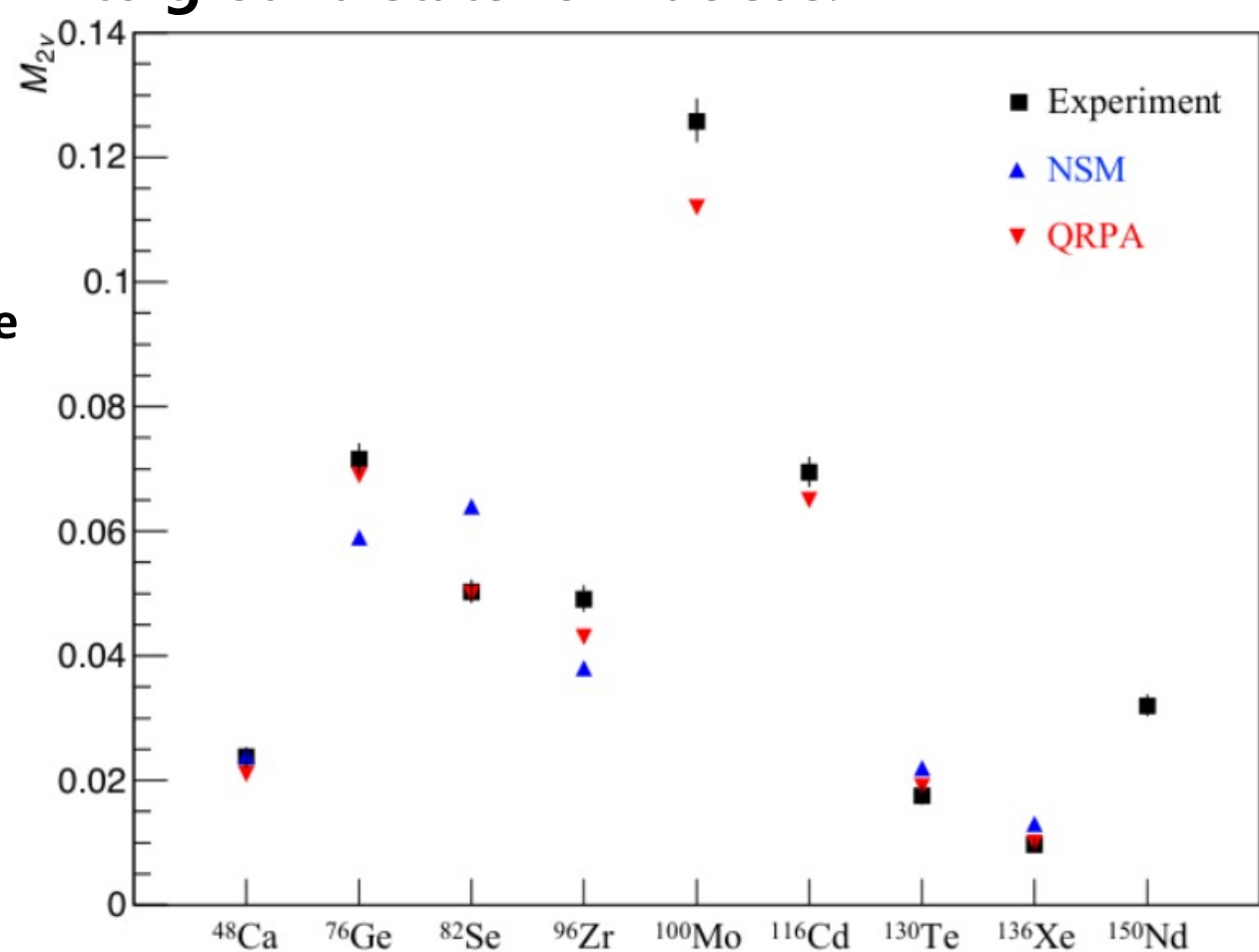
$G_{2\nu}$  : Phase space factor  
 $M^{2\nu}$  : Nuclear Matrix Element (NME)

$$M^{2\nu} = \langle f | O_x | m \rangle \langle m | O_x | i \rangle$$

$i), m), f)$ : initial, mediate, final eigenstate function  
 $O_x$ : transition operator

Due to the dependence of the calculated NME on the nuclear structure model, experimentally measured half lives of  $2\nu\beta\beta$  decay transitions to various energy states in different isotopes can provide valuable input for nuclear structure model studies.

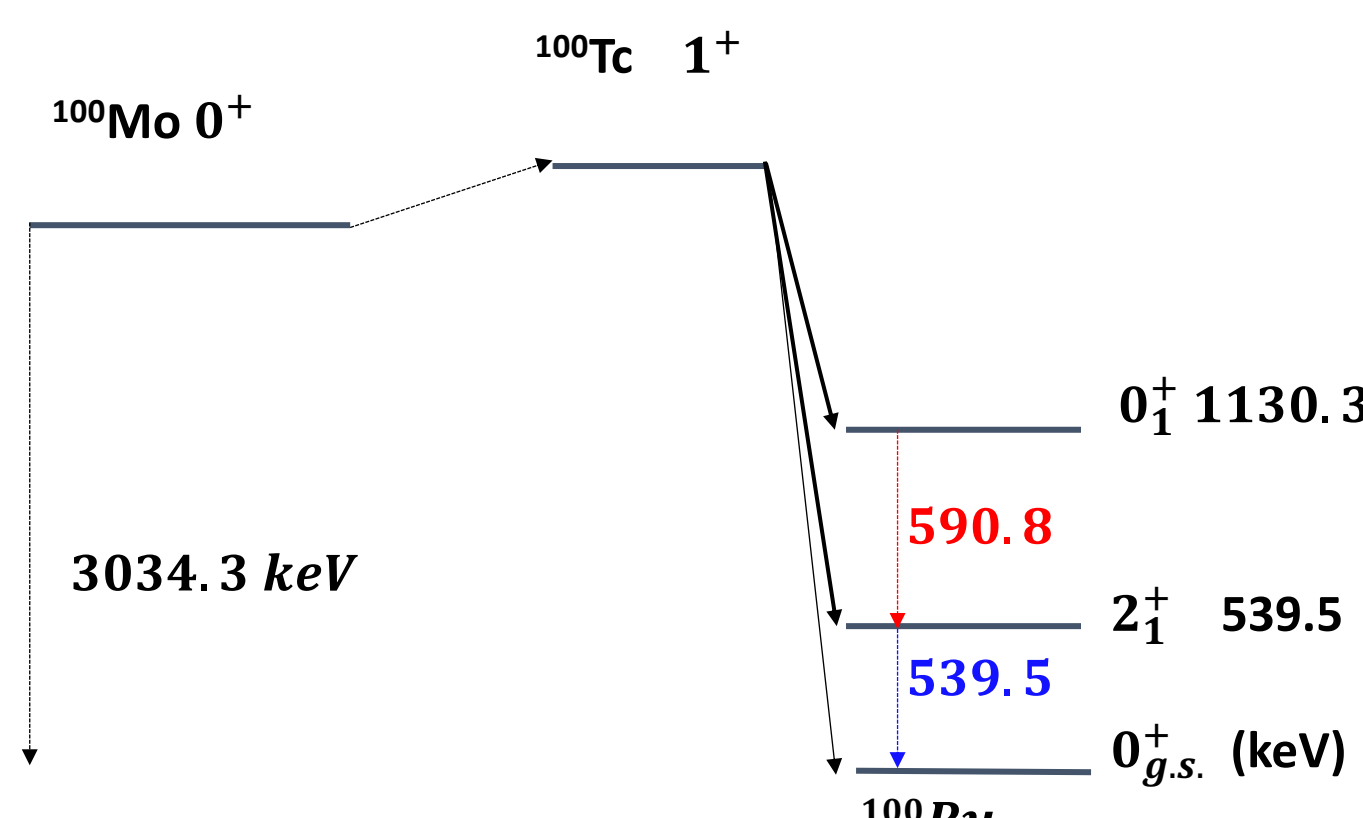
### Theoretically proposed NMEs $2\nu\beta\beta$ decay to ground state for nucleus.



S.Y. Park. Measurements of Double Beta Decay of  $^{100}\text{Mo}$  to the excited States of  $^{100}\text{Ru}$  using HPGe Detectors.

### Half life equation

#### Decay scheme ( $^{100}\text{Mo}$ to $^{100}\text{Ru}$ )



- $^{100}\text{Mo}$  has a natural abundance of 9.7% and can be enriched.
- Due to its high Q-value, the  $2\nu\beta\beta$  ( $0^+ \rightarrow 0^+$ ) decay of  $^{100}\text{Mo}$  to  $^{100}\text{Ru}$  has a measurable half-life.
- $2\nu\beta\beta$  decays to  $\Delta J \neq 0$  excited states study can be sensitive to find the bosonic neutrino.

[ A. S. Barabash, et al., Nucl. Phys. B 783, 90 (2007)

#### Half life table of $2\nu\beta\beta$ to ground state

Nucleus	Average Value ( $T_{1/2}^{2\nu}$ ) [year]
$^{48}\text{Ca}$	$5.3^{+1.2}_{-0.8} \times 10^{19}$
$^{76}\text{Ge}$	$1.88 \pm 0.08 \times 10^{21}$
$^{82}\text{Se}$	$0.87^{+0.02}_{-0.01} \times 10^{20}$
$^{96}\text{Zr}$	$2.3 \pm 0.2 \times 10^{19}$
$^{100}\text{Mo}$	$7.06^{+0.15}_{-0.13} \times 10^{18}$
$^{116}\text{Cd}$	$2.69 \pm 0.09 \times 10^{19}$
$^{130}\text{Te}$	$7.91 \pm 0.21 \times 10^{20}$
$^{136}\text{Xe}$	$2.18 \pm 0.05 \times 10^{21}$
$^{150}\text{Nd}$	$8.4 \pm 1.1 \times 10^{18}$

#### Half life table of $2\nu\beta\beta$ to excited state

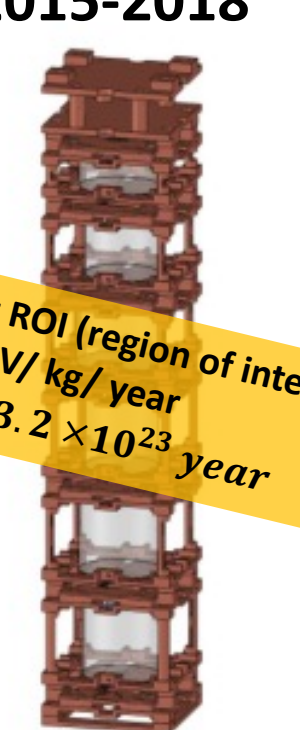
Nucleus	Average Value ( $T_{1/2}^{2\nu}$ ) [year]
$^{150}\text{Nd}$ to ( $0_1^+$ )	$1.2^{+0.3}_{-0.2} \times 10^{20}$
$^{100}\text{Mo}$ to ( $0_1^+$ )	$6.7^{+0.5}_{-0.4} \times 10^{20}$

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## $2\nu\beta\beta$ decay to excited states of $^{100}\text{Mo}$ and AMoRE

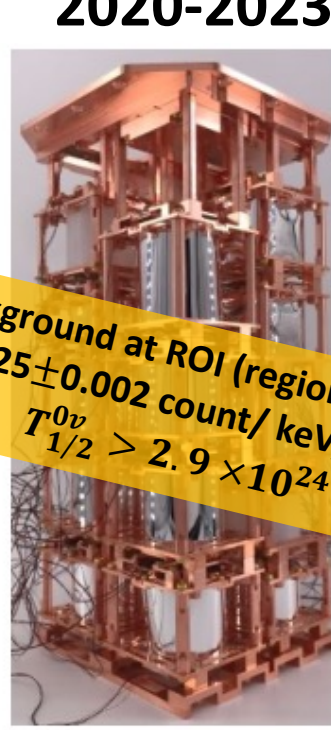
The multi-crystal hit condition enabled by AMoRE's multi-detector structure offers an advantage for studying  $2\nu\beta\beta$  decay to excited states.

#### AMoRE-Polit 2015-2018



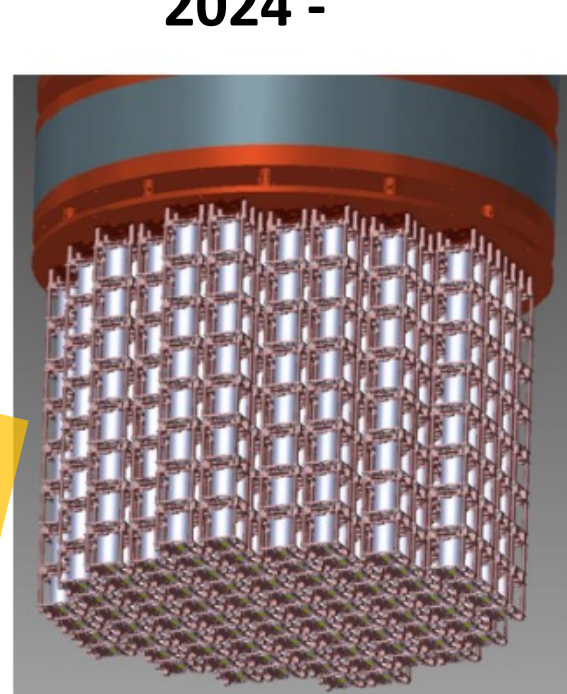
Background at ROI (region of interest)  $\sim 0.5$  count/keV/kg/year  
 $T_{1/2} > 3.2 \times 10^{23}$  year

#### AMoRE-I 2020-2023



Background at ROI (region of interest)  $\sim 0.025 \pm 0.002$  count/keV/kg/year  
 $T_{1/2} > 2.9 \times 10^{23}$  year

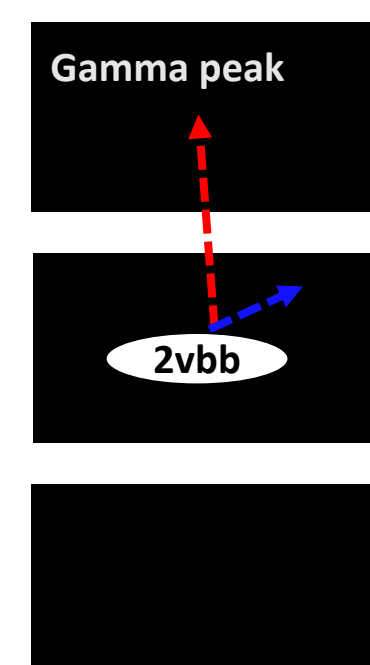
#### AMoRE-II 2024 -



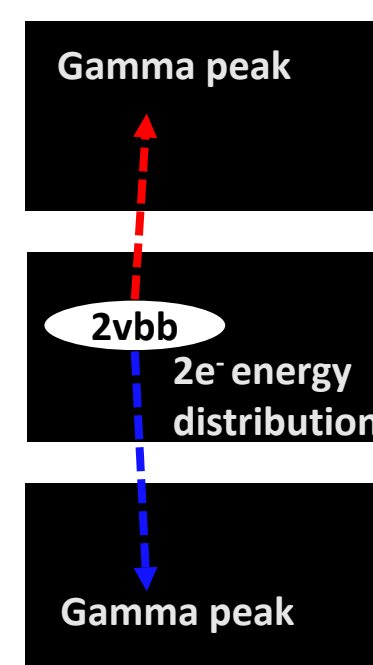
- ✓ 157 kg of XMO
- ✓ Expected exposure > 500  $\text{kg}^{100}\text{Mo} \cdot \text{yr}$
- ✓ In Yemilab

#### Schematics of multi crystal hit

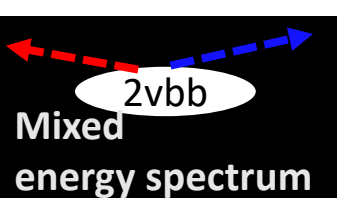
##### Double crystal hit



##### Triple crystal hit

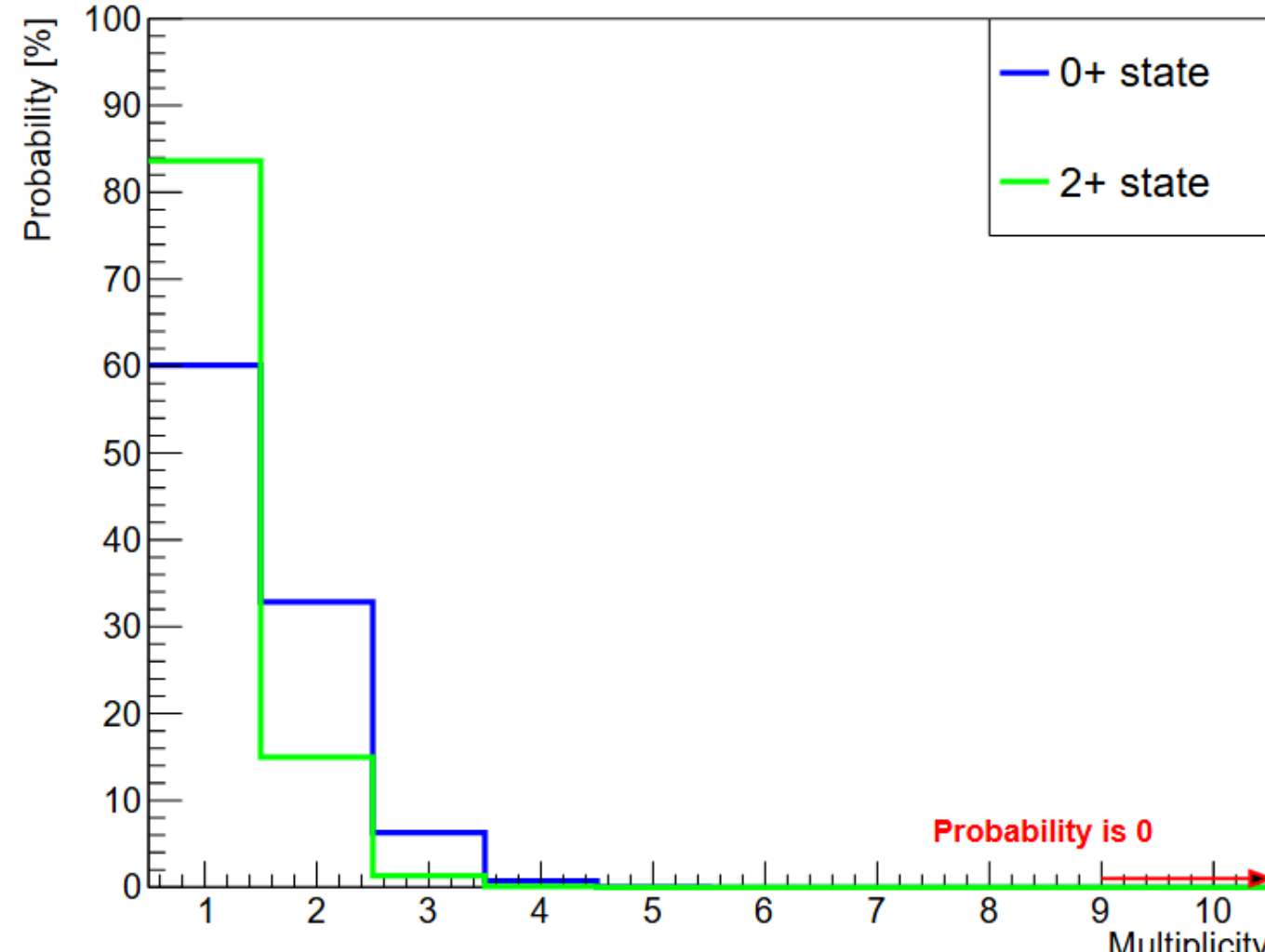


##### Single crystal hit

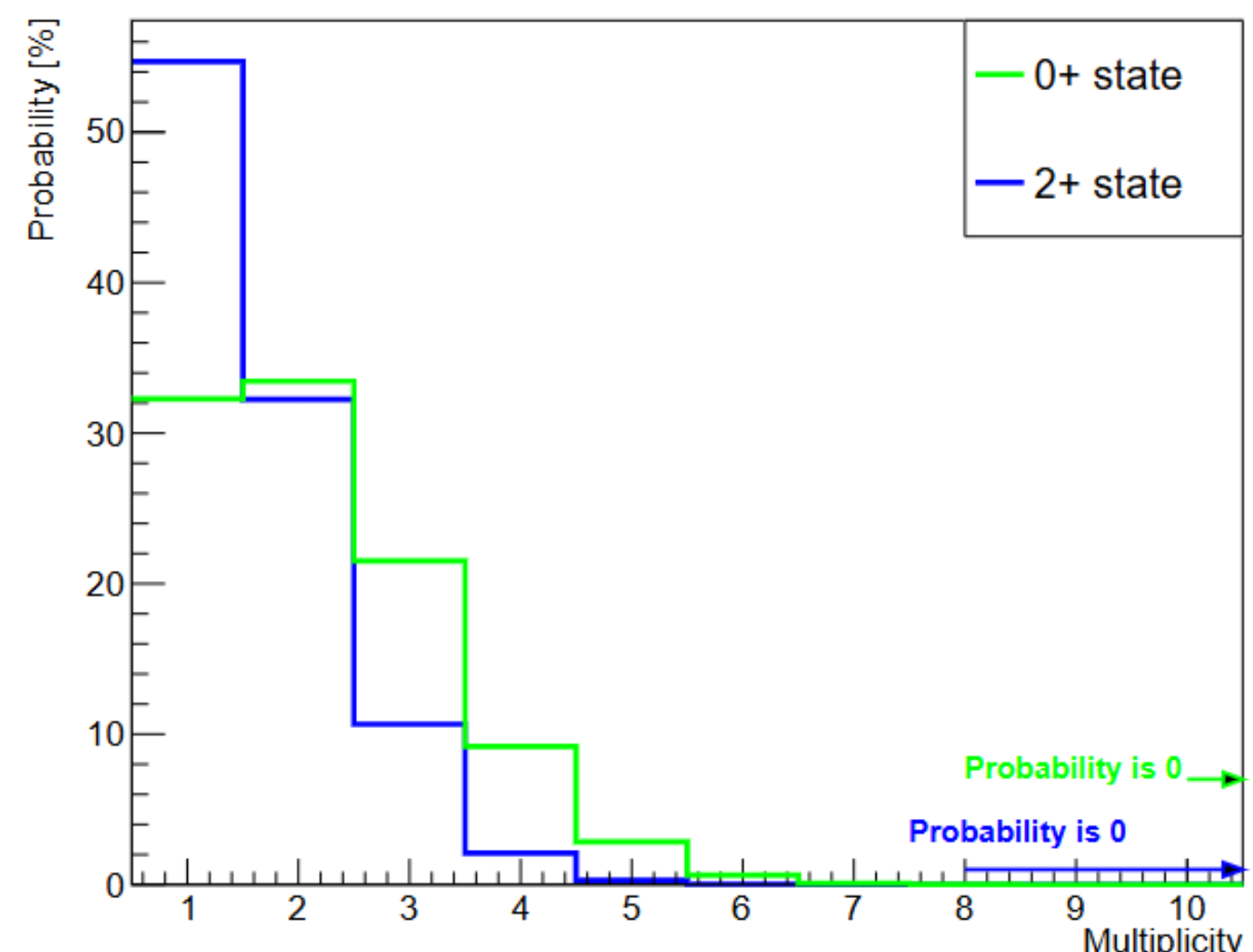


#### Probability of a multi-crystal hit (Geant4 simulation)

##### The probability histogram at each multiplicity at AMoRE-I



##### The probability histogram at each multiplicity at AMoRE-II



## AMoRE-I: Study of $2\nu\beta\beta$ decay to excited states

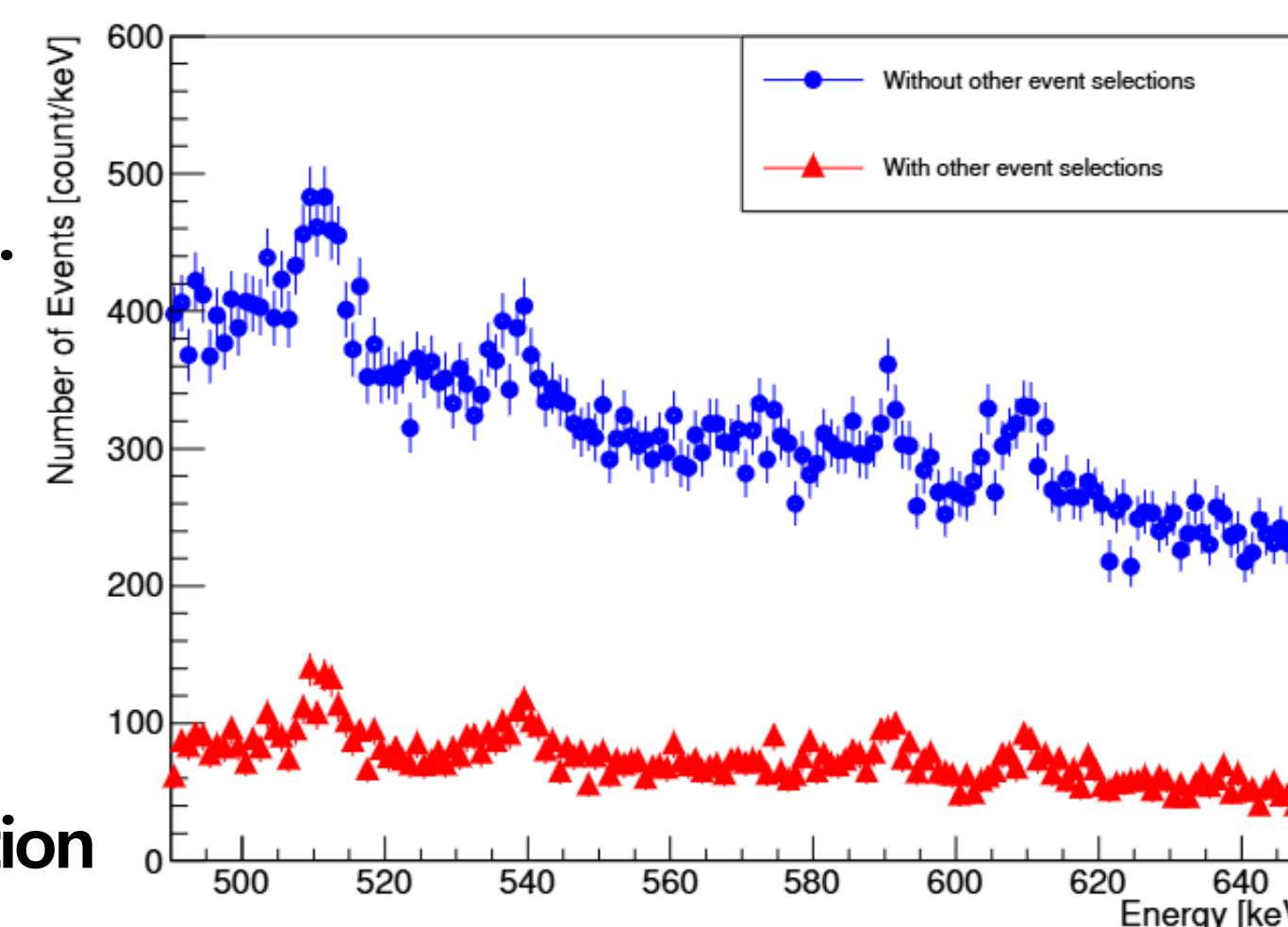
### Data

- 486.6 days of PROD data were analyzed.
- SE02 and LMO2 crystals were excluded.
- Only double crystal hit events were considered.
  - Double crystal hit probability: 32.9%
  - Triple crystal hit probability: 6.3%

### Process

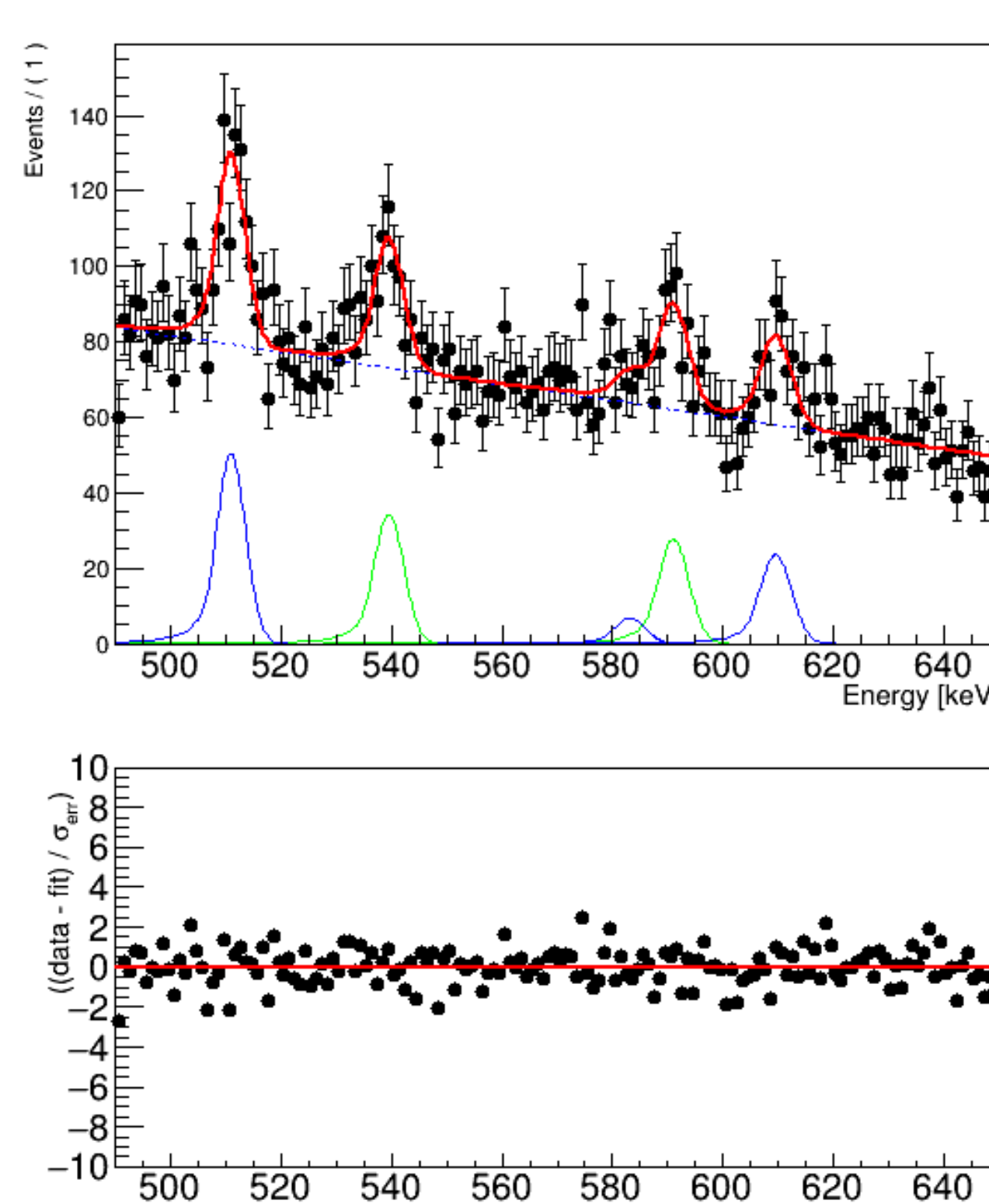
- Event selections
  - Muon tagging
  - Position
  - Energy
  - Signal time difference
- Calibrations
  - Energy calibration
  - Signal time calibration

#### Double-hit event energy distribution



## AMoRE-I results: Study of $2\nu\beta\beta$ decay the $0_1^+$ state

### Fit histogram



### The log-likelihood fit with the Gaussian constraints

$$\mathcal{L} = \frac{Y^N e^{-Y}}{N!} \prod_i P_i^{total} \prod_j e^{-\frac{1}{2} \frac{P_j^2}{\sigma_j^2}}$$

$$P_i^{total} = \frac{1}{Y} \left( Y_{540} P_{i,540}^{cb} + Y_{591} P_{i,591}^{cb} + Y_{511} P_{i,511}^{cb} + Y_{583} P_{i,583}^{cb} + Y_{609} P_{i,609}^{cb} + Y_{pol} P_i^{pol} \right)$$

where,  
 $Y_{pol} = Y - (Y_{540} + Y_{591} + Y_{511} + Y_{583} + Y_{609})$

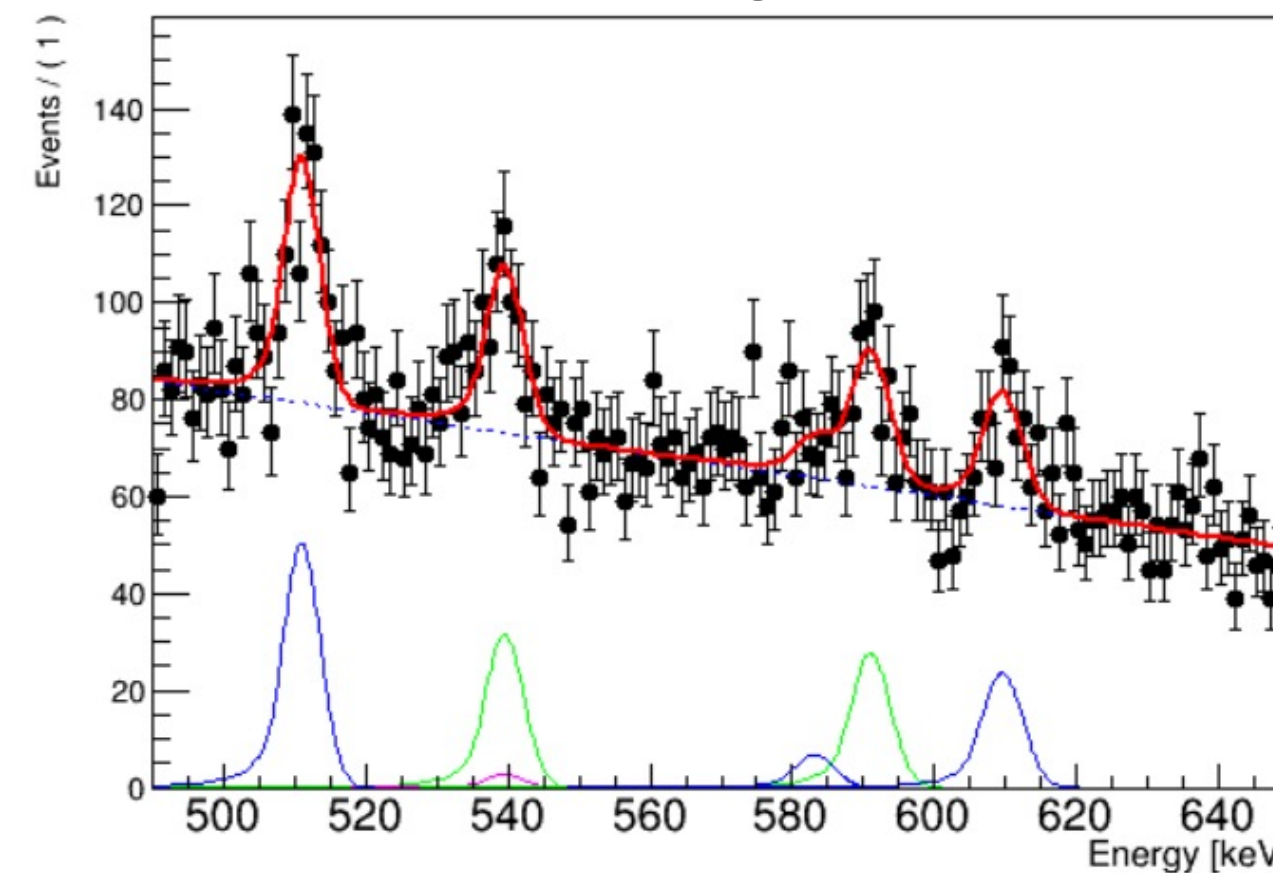
### Results table of Study of $2\nu\beta\beta$ decay to excited states of $^{100}\text{Mo}$

AMoRE-I	Results [ $\times 10^{20}$ year] $\pm$ stat $\pm$ sys
539.5 keV	$6.57 \pm 0.91 \pm 0.34$
591.8 keV	$7.13 \pm 1.10 \pm 0.32$
weighted average	$6.83 \pm 0.71 \pm 0.32$
Soudan(95)	$6.1 \pm 1.8$
Soudan(99)	$9.3^{+2.8}_{-1.7} \pm 1.4$
TUNL-ITEP(01)	$5.9^{+1.7}_{-1.1} \pm 0.6$
TUNL-ITEP(06)	$6.0^{+1.9}_{-1.1} \pm 0.6$
Modane(07)	$5.7^{+1.3}_{-0.9} \pm 0.8$
TUNL-ITEP(09)	$5.5^{+1.2}_{-0.8} \pm 0.3$
ARMONIA(10)	$6.9^{+1.0}_{-0.8} \pm 0.7$
Modane(14)	$7.5 \pm 0.6 \pm 0.6$
Average	$6.7^{+0.5}_{-0.4}$
CUPID-Mo(23)	$7.5 \pm 0.8^{+0.4}_{-0.3}$

A.S.Barabash et al (1995, 1999); Braeckeleer et al (2001); R.Arnold et al (2007); M.F.Kidd et al (2009); P.Belli et al (2010); R.Arnold et al (2014).

## AMoRE-I results: Study of $2\nu\beta\beta$ decay to the $2_1^+$ state

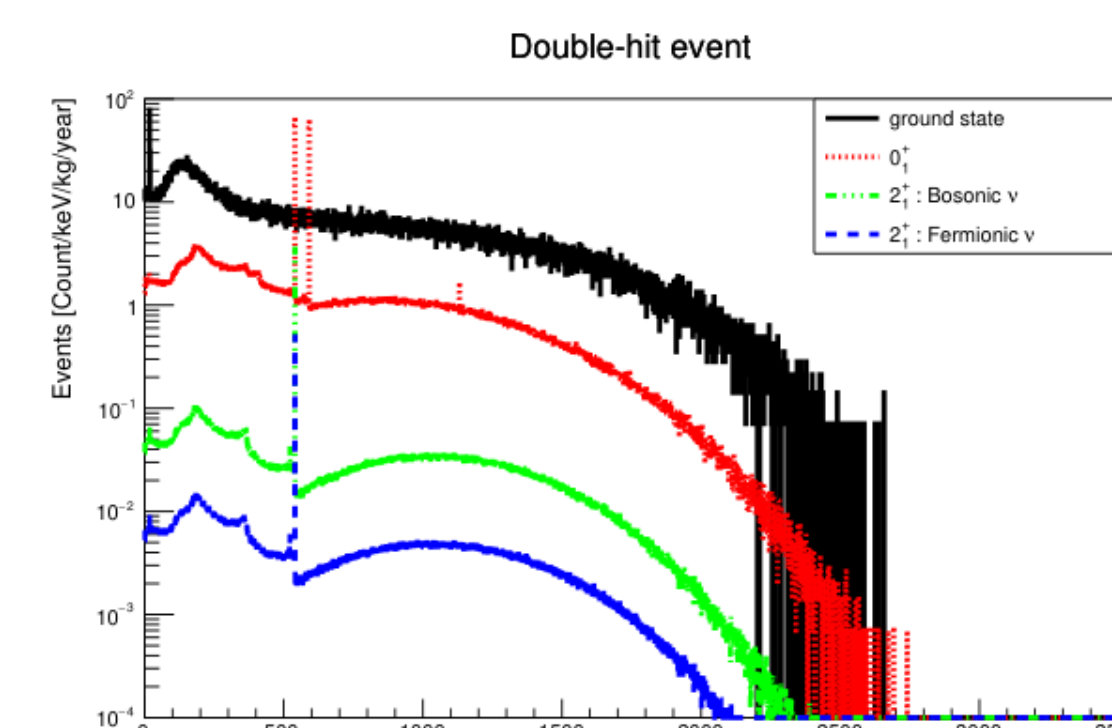
### Fit histogram



$$P_i^{total} = \frac{1}{Y} \left( \epsilon_{540}^{0_1^+} \times Y_{591}^{0_1^+} P_{i,540}^{cb} + Y_{591}^{0_1^+} P_{i,591}^{cb} + Y_{540}^{2_1^+} P_{i,540}^{cb} + Y_{511} P_{i,511}^{cb} + Y_{583} P_{i,583}^{cb} + Y_{609} P_{i,609}^{cb} + Y_{pol} P_i^{pol} \right)$$

Half-life limit:  
 $2.5 \times 10^{21}$  year(90% c.i.)

## Prospective study of $2\nu\beta\beta$ to excited states at AMoRE-II

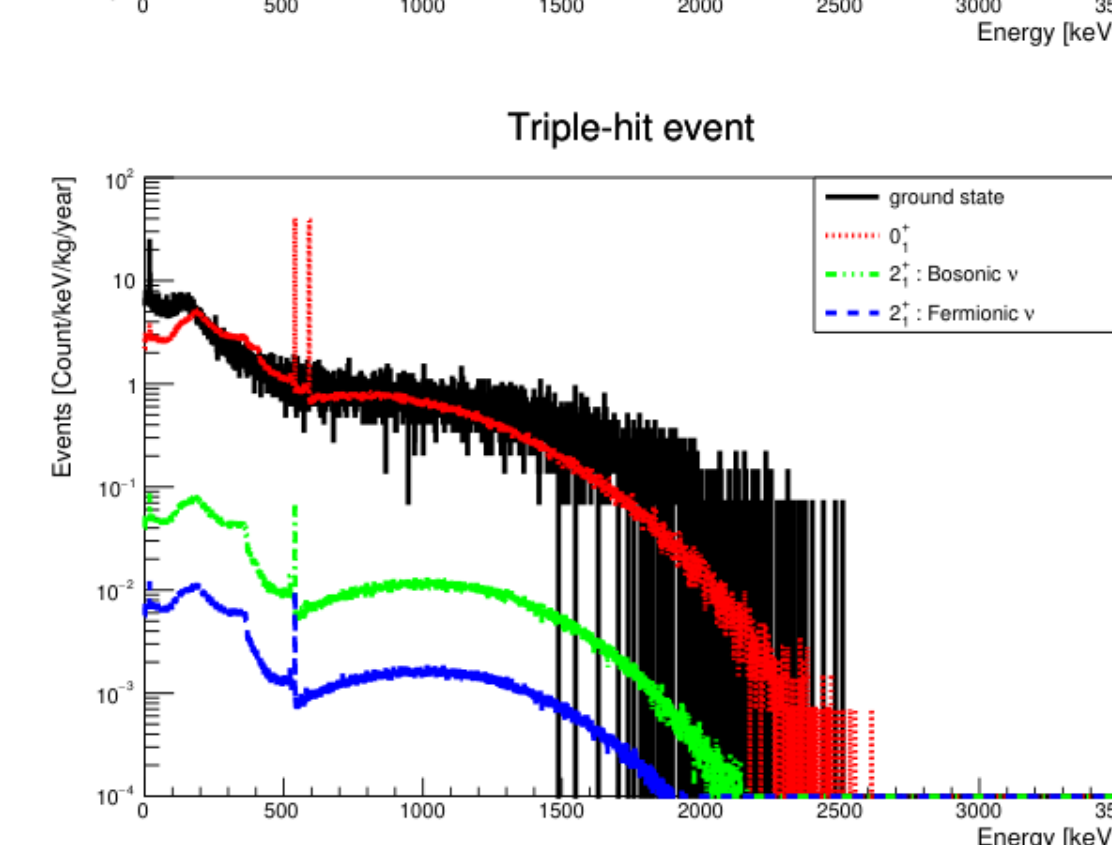


### Probability improvement

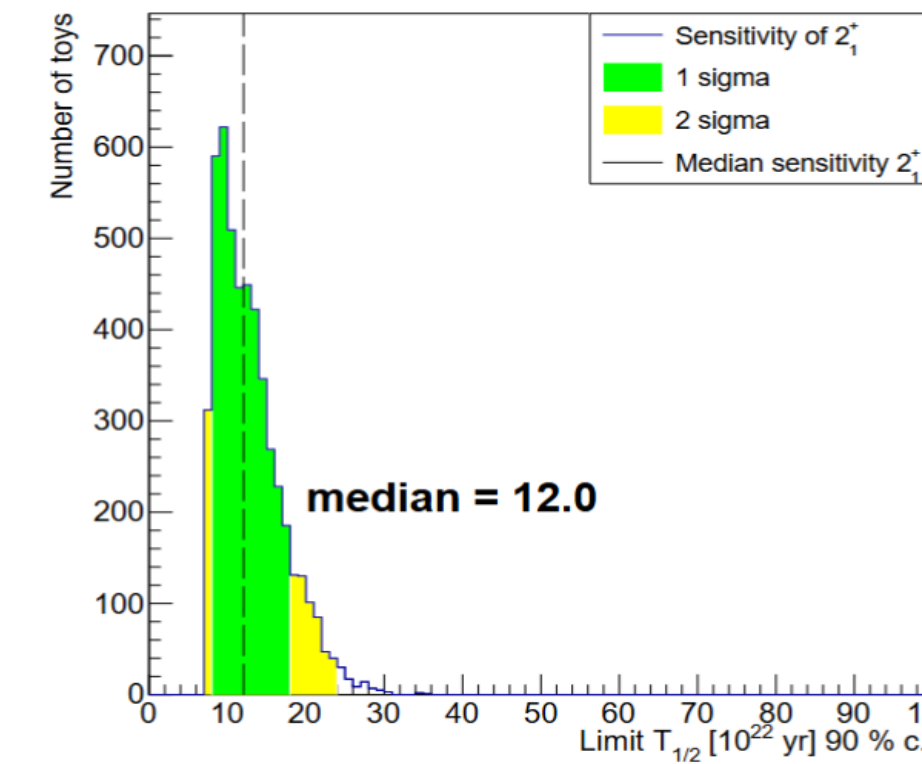
- Probability of  $2\nu\beta\beta$  to  $0^+$ 
  - Double crystal hit: 33.4% (32.9%)
  - Triple crystal hit: 21.5% (6.3%)
- Probability of  $2\nu\beta\beta$  to  $2^+$ 
  - Double crystal hit: 32.2% (15.0%)
  - Triple crystal hit: 10.7% (1.3%)

### Statistical improvement

- Ratio of the error to 540 keV peak count at  $2\nu\beta\beta$  to  $0^+$ :  $\sim 0.3\%$  (AMoRE-I:  $\sim 6.3\%$ )



### Sensitivity for $2\nu\beta\beta$ to $2_1^+$



### The conceptual equation

$$N_{540 \text{ keV}}^{2+} = N_{540 \text{ keV}}^{tot} - N_{540 \text{ keV}}^{0+}$$

Expected Half-life limit:  
 $1.20 \times 10^{23}$  year(90% c.i.)

## Summary

### study of $2\nu\beta\beta$ to excited states at AMoRE-II

AMoRE-I: $0_1^+$ state	Results [ $\times 10^{20}$ year] $\pm$ stat $\pm$ sys
539.5 keV	$6.57 \pm 0.91 \pm 0.34$
591.8 keV	$7.13 \pm 1.10 \pm 0.32$
weighted average	$6.83 \pm 0.71 \pm 0.32$
AMoRE-I: $2_1^+$ state	$> 25$ (90% c.i.)

### Prospective study of $2\nu\beta\beta$ to excited states at AMoRE-II

- In AMoRE-II, we can observe the triple-hit signal generated by  $2\nu\beta\beta$  to  $0^+$ .
- The statistical error of the half-life of  $2\nu\beta\beta$  to  $0^+$  will be reduced by approximately a factor of 0.05.
- The sensitivity of  $2\nu\beta\beta$  to  $2^+$  at AMoRE-II is  $> 1.20 \times 10^{23}$  year.